

Philosophy 230
Wesleyan University
Fall 2014
Handout 2b
Polyadic Paraphrase

I. Relative scopes and differences in truth conditions

- A. Everyone loves someone.
- B. Someone is loved by everyone.

II. Logical Forms

- A. Every statement has one of seven kinds of logical forms:

- 1. $(\forall x)(\dots x \dots)$
- 2. $(\exists x)(\dots x \dots)$
- 3. $\neg(\dots)$
- 4. $(\dots)(\dots)$
- 5. $(\dots) \vee (\dots)$
- 6. $(\dots) \supset (\dots)$
- 7. $(\dots) \equiv (\dots)$

- B. If a statement has one of the first two of these forms, then we say that it has a *quantificational* form at the highest level.
- C. In particular, we say that it is a universal quantification, or an existential quantification at the highest level.
- D. If a statement has the next 5 forms, then we say that it has a *truth-functional* form at its highest level.
- E. In particular, we say that the statement is a negation, or conjunction, or disjunction, or conditional, or biconditional, at the highest level.

III. Polyadic paraphrase:

- A. If John likes someone, then everyone does.
- B. Every student dislikes some class.
- C. If every class disliked by someone is liked by someone, then no class is disliked by everyone.

IV. Definition of monadic schemata

- A. (*Monadic*) *open schemata*:

- 1. (*Monadic*) *atomic open schema*: e.g.,
 Fx, Gy , etc.
- 2. A (*monadic*) *complex open schema*: e.g.,
 $Fx.Gx \supset Hx$

3. Note that **only one** free variable is allowed.

B. *Simple monadic schema*: e.g.,

$$(\exists x)(Fx \equiv Gx),$$

$$(\forall y)(Hy.(Gy \vee Fy))$$

C. *Pure monadic schema*: e.g.,

$$(\exists x)(Fx \equiv Gx) \supset (\forall y)(Hy.(Gy \vee Hy))$$

D. *Monadic schema*: e.g.,

$$(\forall x)(Fx \supset Gx \vee Hx) \supset Fx$$